

beyond agent-based and spatial interaction
INTERACTION BASED COMPUTING

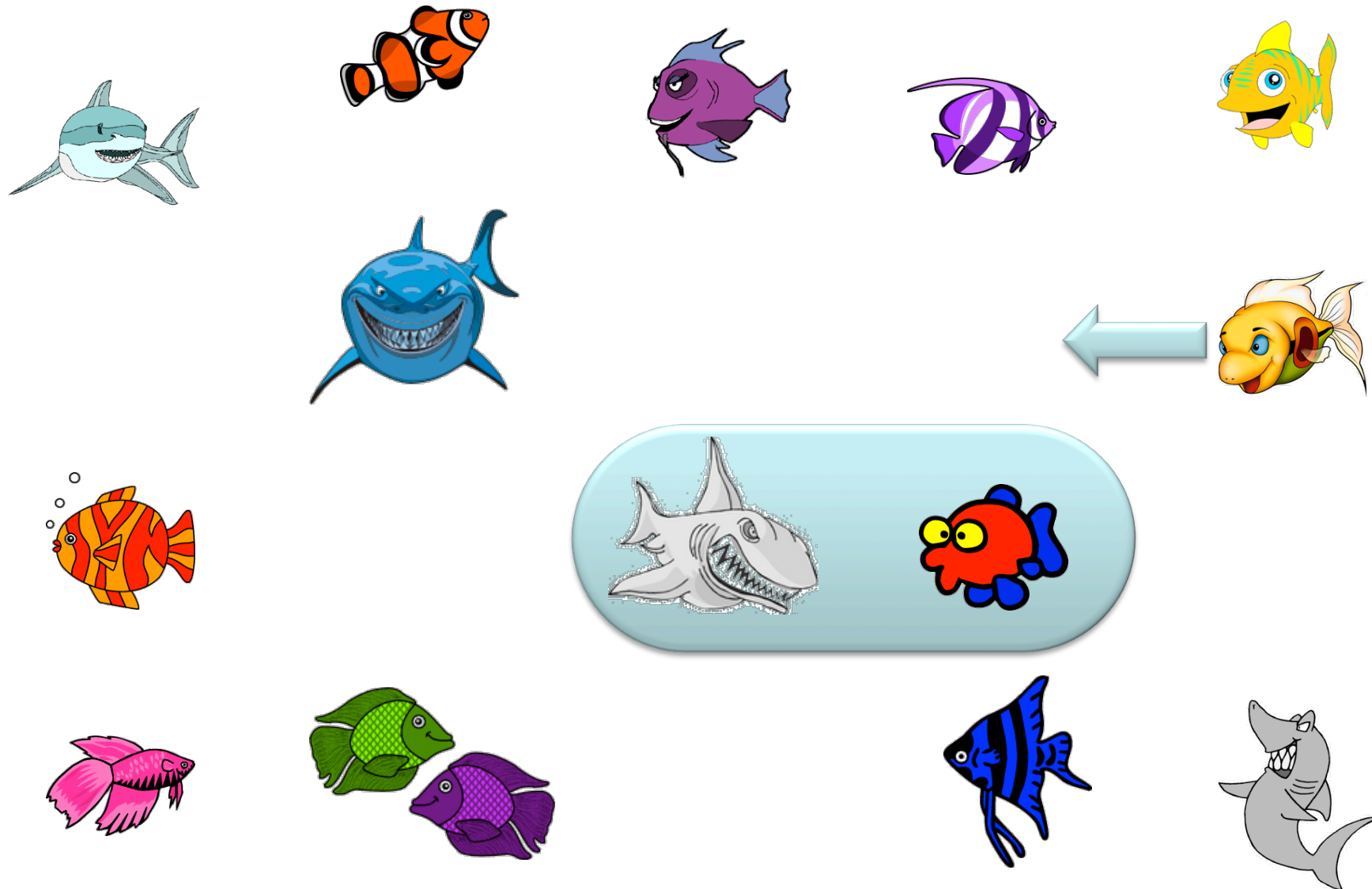
Space-Centric, Agent-Centric and Interaction-Oriented Modeling

(in the previous example of languages there are)

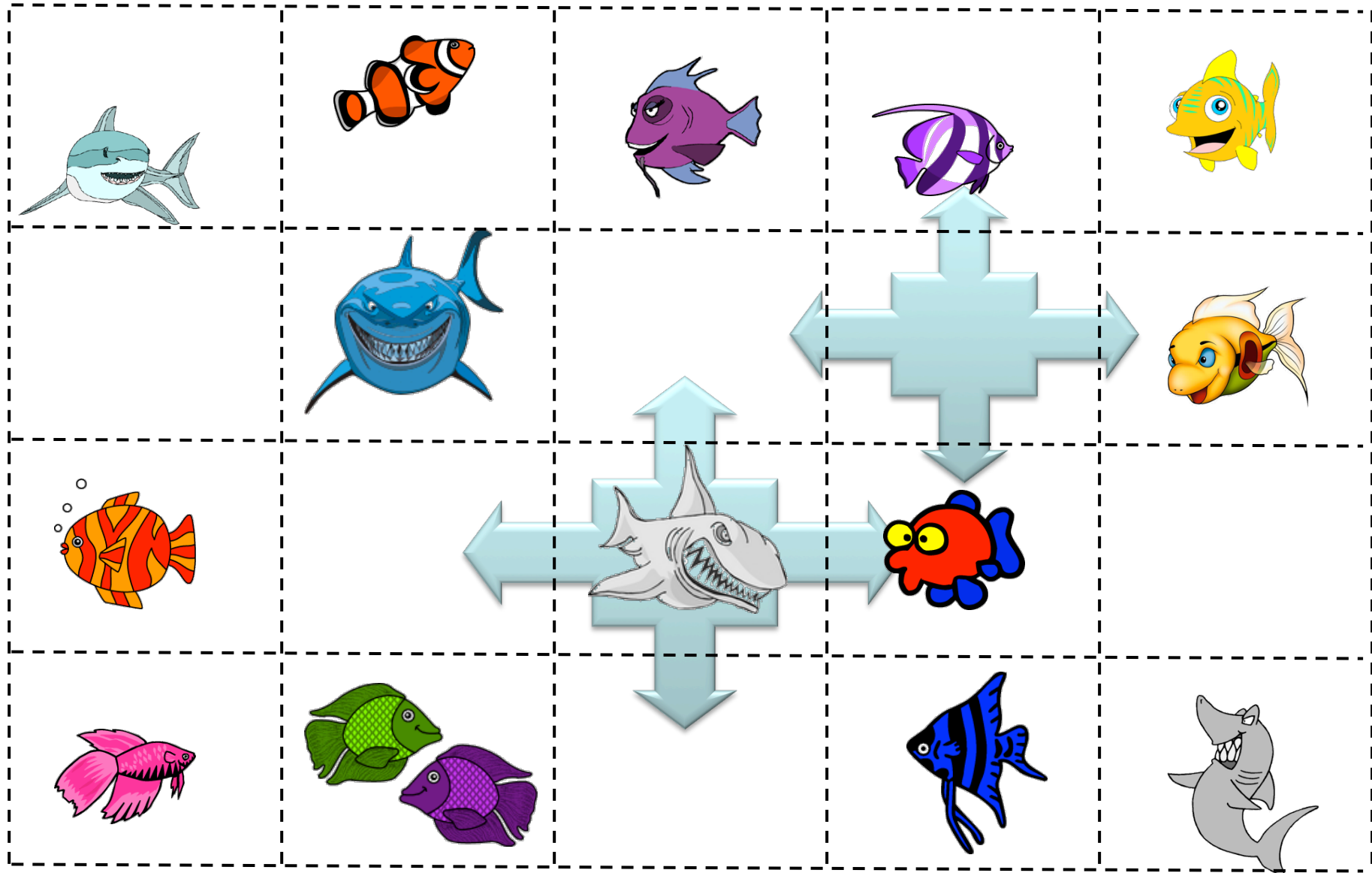
Two main modeling approaches

- agent-based
- space-based

Fish and Sharks in the sea (agent-based view)



Fish and Sharks in the sea (space-centric view)

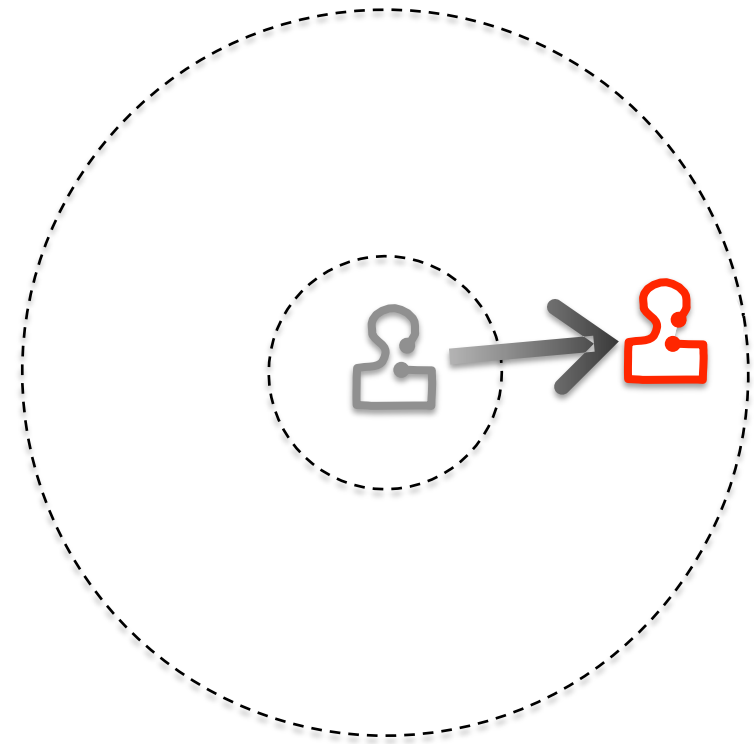


Space-Centric, Agent-Centric and Interaction-Oriented Modeling

(in the previous example of languages there are)

Two main modeling approaches

- agent-based
 - the structure of the system is described through its **components** (agent, entity) *not through its processes*
 - an agent evolves by **receiving a message** from *one* other agent

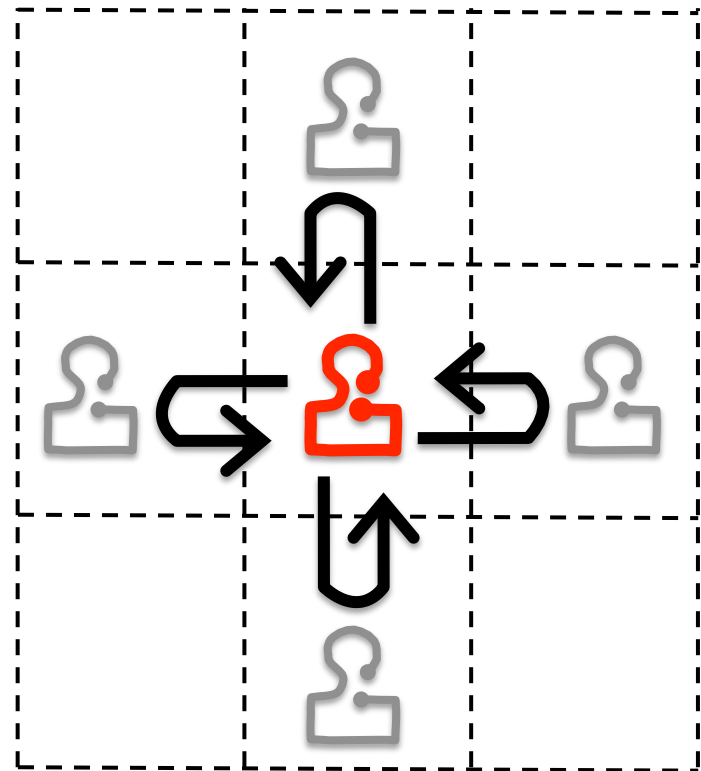


Space-Centric, Agent-Centric and Interaction-Oriented Modeling

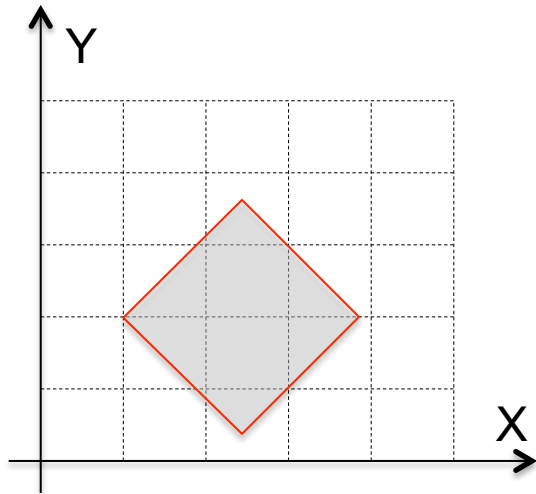
(in the previous example of languages there are)

Two main modeling approaches

- space-based
 - the structure of the system is described through its **spatial domain**
not through its processes
 - an “elementary piece of space” evolves by **querying** the neighborhood



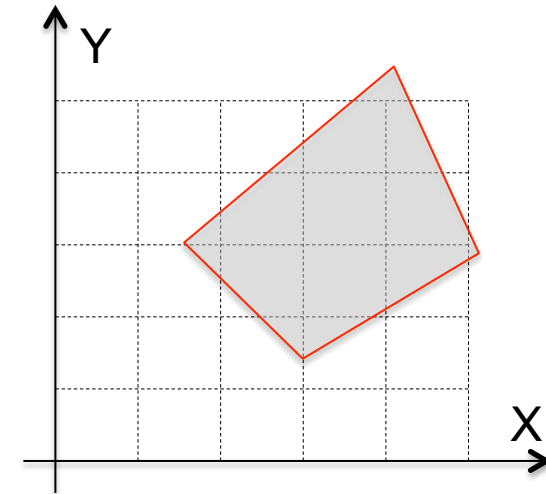
Same distinction for continuous models (fluid dynamics)



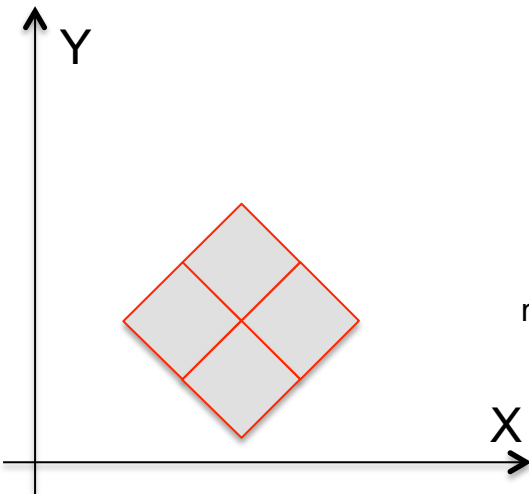
state t

Eulerian mesh

what is occurring at a fixed point in a reference frame as time progresses (as in cellular automata)

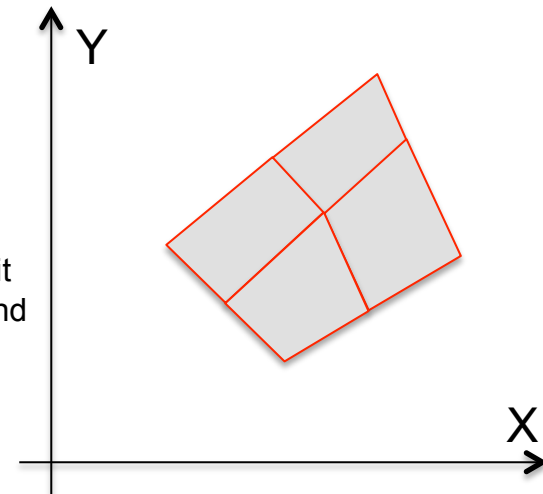


state $t+1$



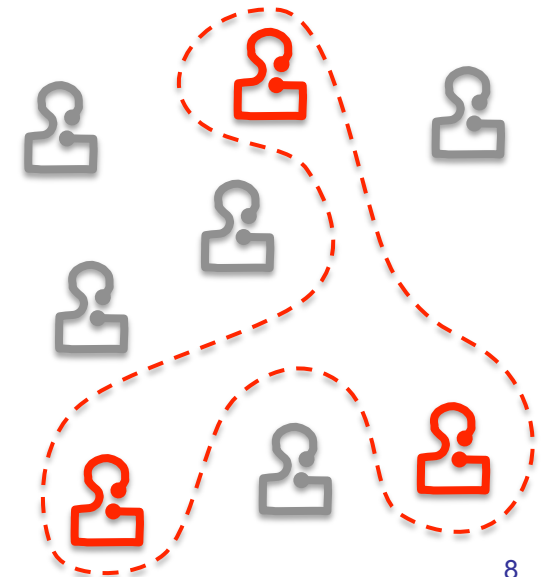
Lagrangian mesh

follows the position (and other properties) of a spatial element as it moves through a reference space and time (as in agent-based models)



A shift in perspectives

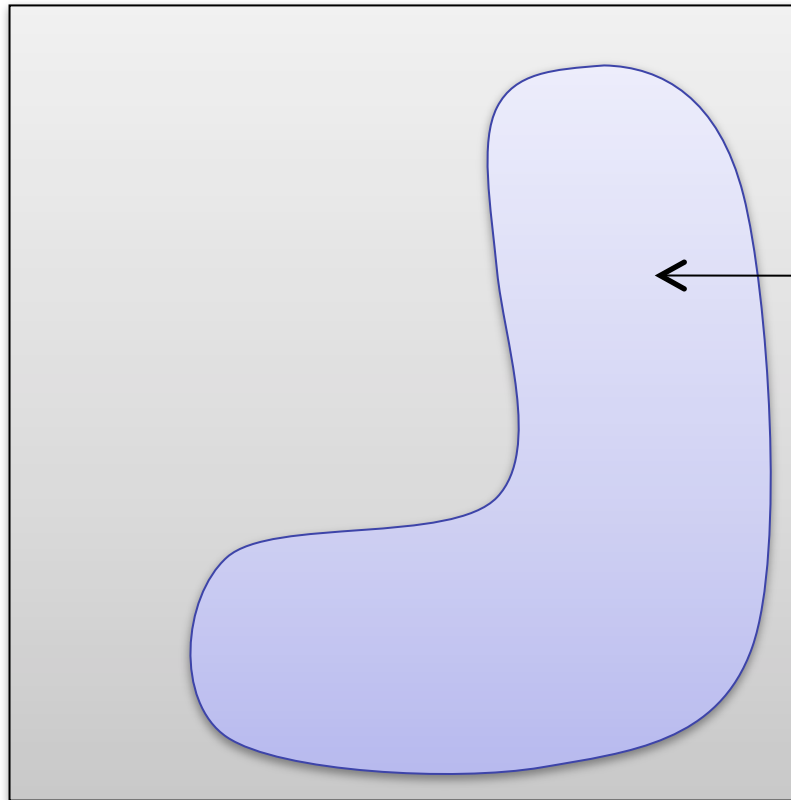
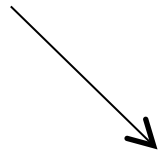
- the distinction impacts the language level
(agent based and object oriented languages vs. spatial computing languages)
- The distinction vanishes for dynamic structure
(agent and “piece of space” creation, rearrangement and deletion)
- *Neither framework is satisfactory*
because they focus on the evolution of **one**
entity
- A **subsuming view** is possible:
interaction-based structuration



The Topological Structure of Interactions

Decompose a system into subsystems following the elements in interaction

A system in some state

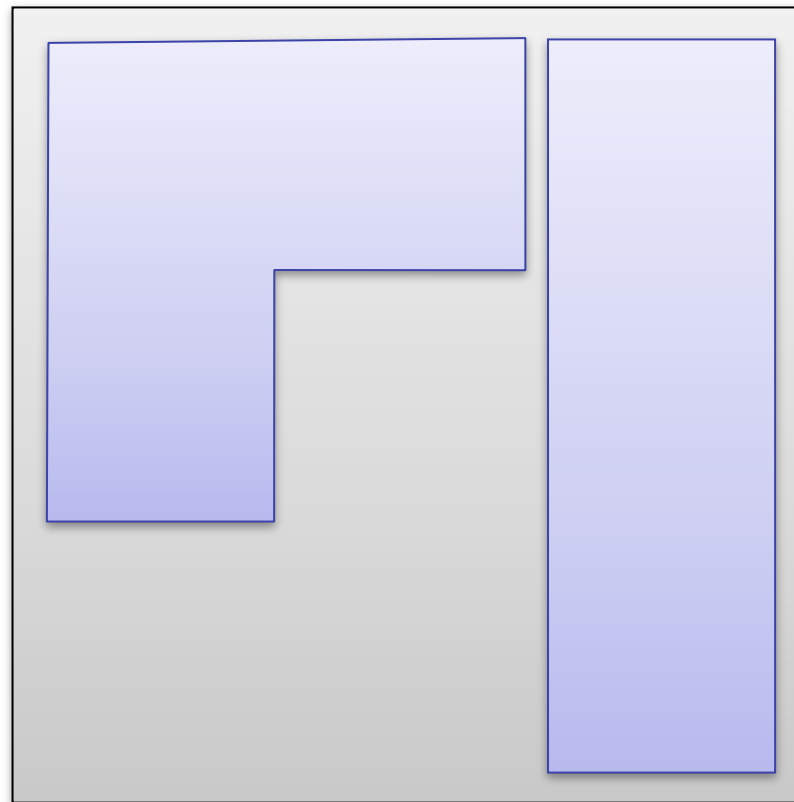


*Part of a system
that evolves.*

*Can be identified
by comparison
with the previous
global state*

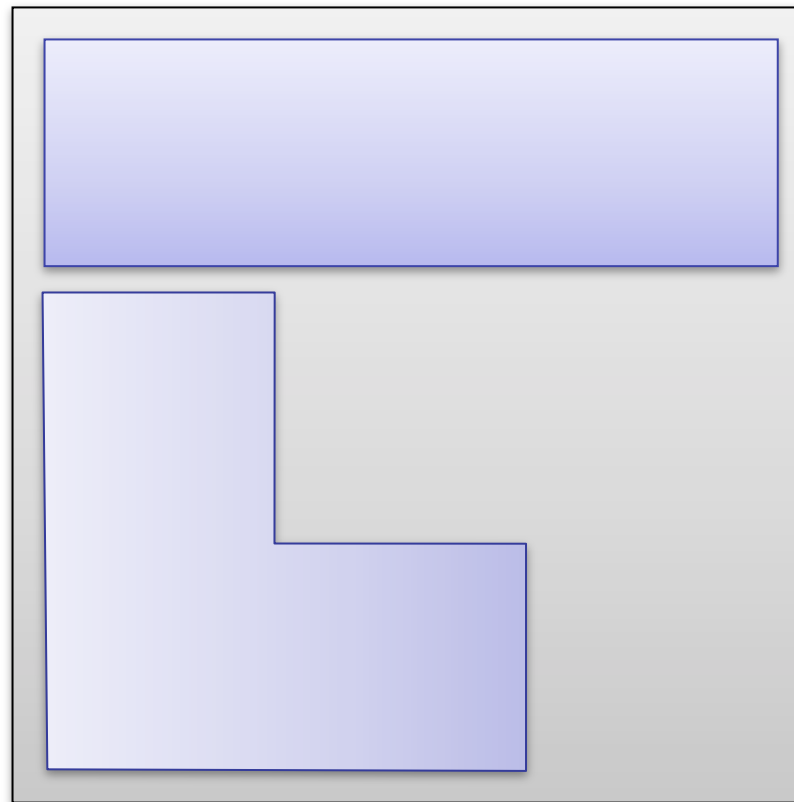
Decompose a system into subsystems following the elements in interaction

$t = 1$



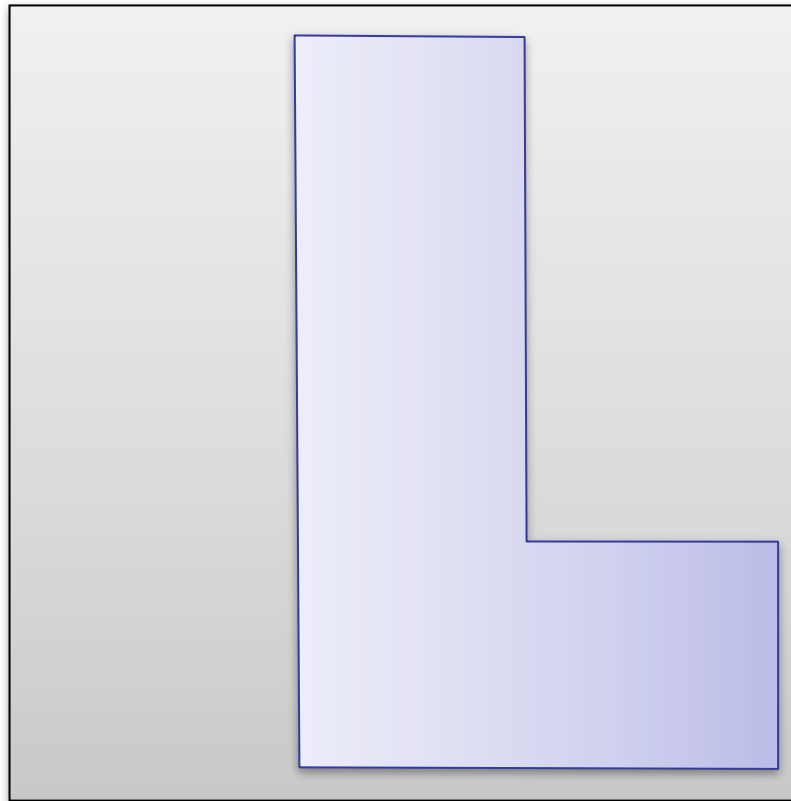
Decompose a system into subsystems following the elements in interaction

$t = 2$

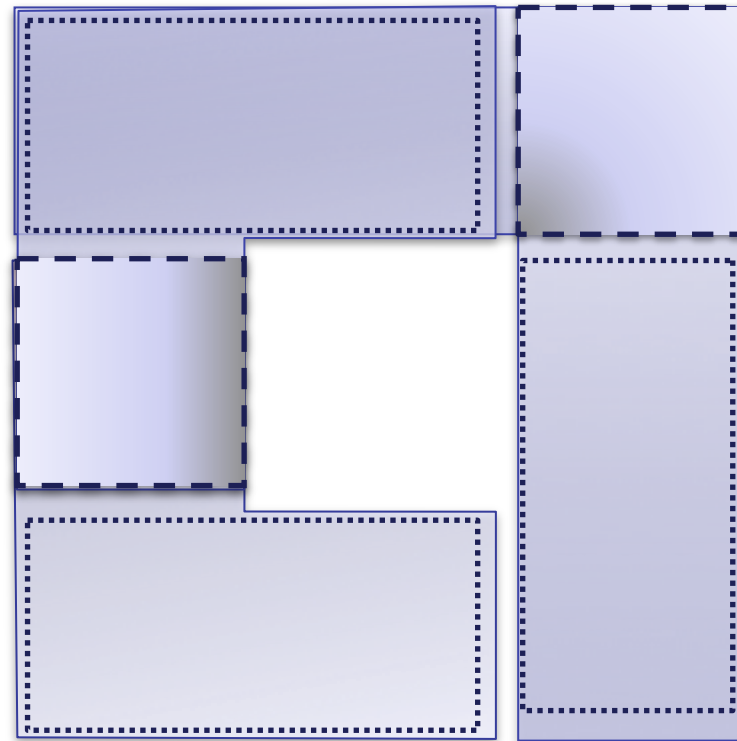


Decompose a system into subsystems following the elements in interaction

$t = 3$

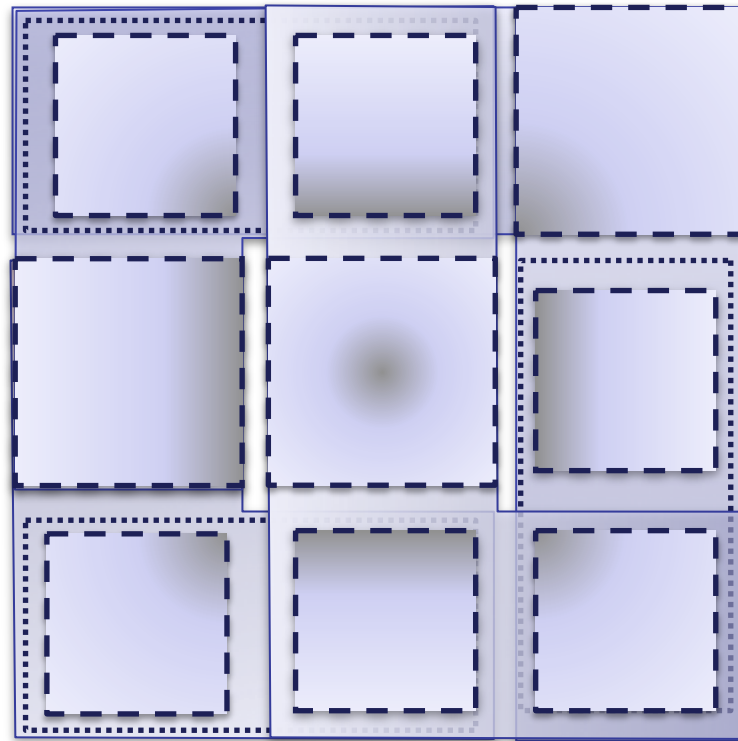


Decompose a system into subsystems following the elements in interaction

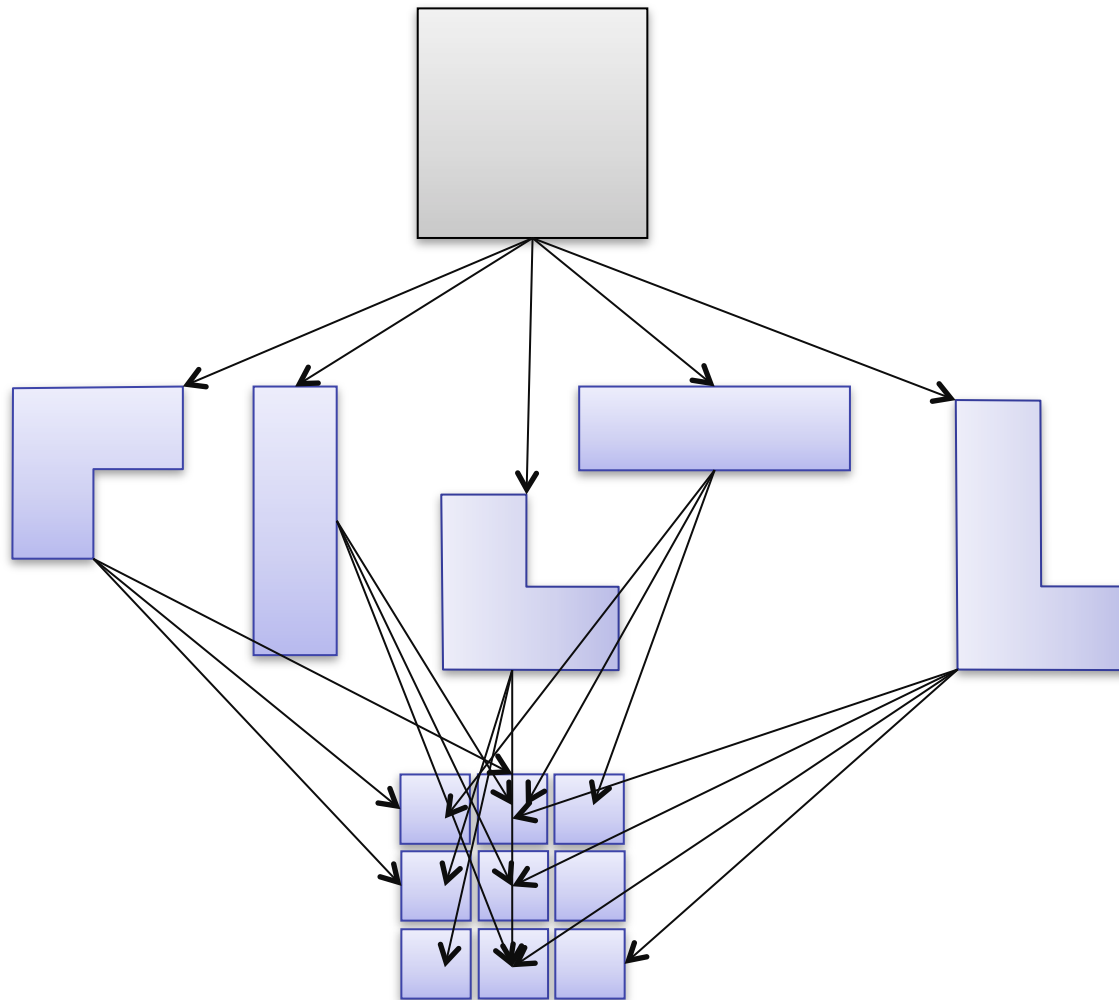


Decompose a system into subsystems following the elements in interaction

The interactions decomposes the systems into elementary parts.
An interaction implies one or several elementary parts.



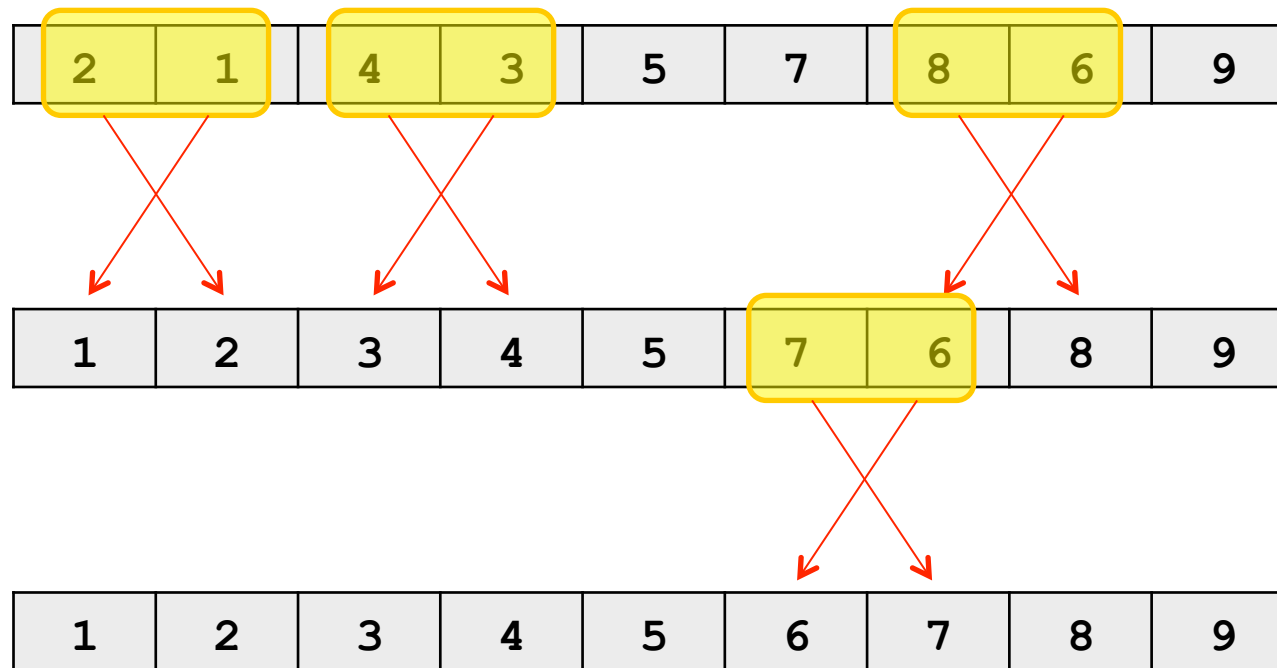
Decompose a system into subsystems following the elements in interaction



the inclusion structure
between the elementary
and interacting parts is
a lattice

a (simplicial) complex
is a better (topological)
equivalent
representation

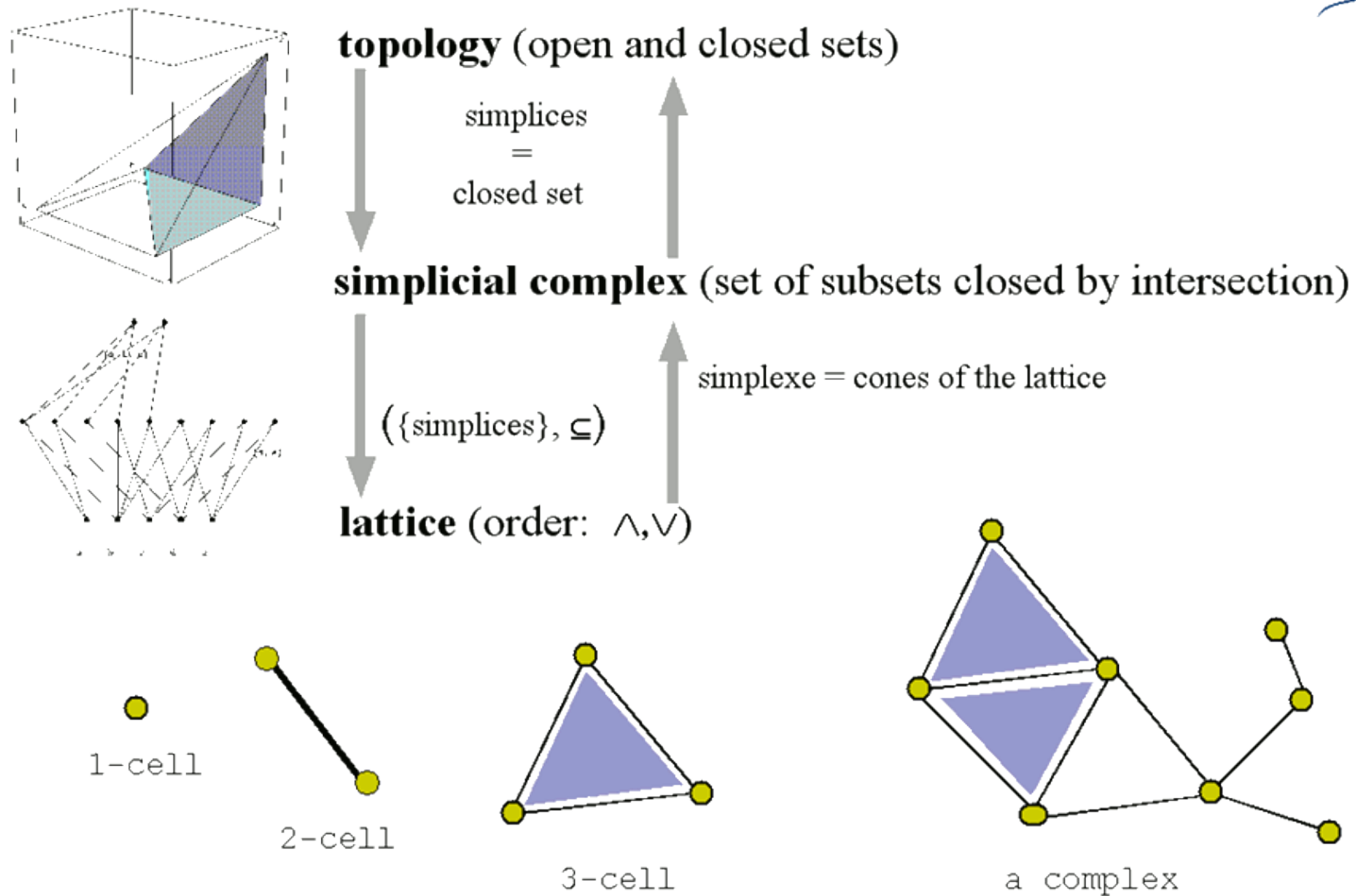
The space of bubble-sort



Bubble-sort is a process where:

- the state of the system is a sequence of numbers
 - an interacting part in the system is a pair of adjacent decreasing numbers
 - the transformation of an interacting couple exchanges the couple's elements
 - the topology of the interacting parts is build upon the topology of the sequence
- or*
- the topology of the sequence can be recovered from the possible element's swap

Topology, simplicial complex and lattice



Higher dimensional objects for complex simulations

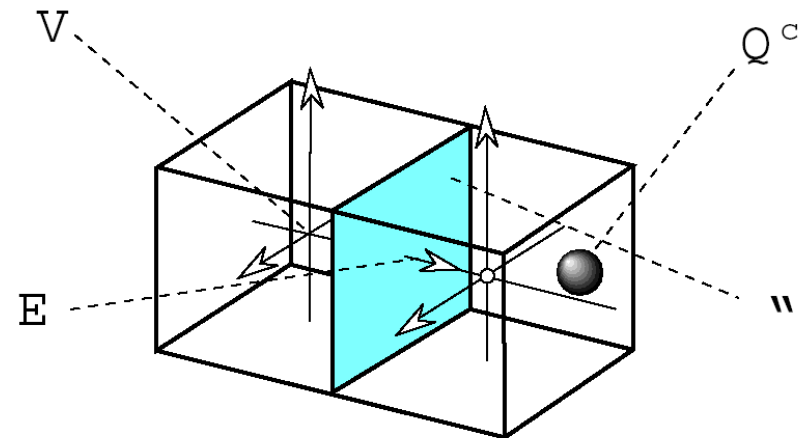
Example of electrostatic Gauss law [Tonti 74]

- Electric charge content ρ : dimension 3
- Electric flux Φ : dimension 2
- Law available on an arbitrary complex domain

$$\phi = \iint w \cdot dS = \frac{Q^c}{\varepsilon_0} = \iiint_{(V)} \frac{\rho}{\varepsilon_0} d\tau$$

electric field in space:

- V: electric potential (dim 0)
- E: voltage (dim 1)
- w: electric flux (dim 2)
- Qc: electric charge (dim 3)



A Direct Discrete Formulation of Field Laws: The Cell Method

The grand picture

1. Describe a dynamical system following the interaction of its parts
2. Each part is characterized by a (local) state
3. The global state of the system is the “sum” of its local state and their topological organization
4. An interaction makes evolve a (small) subset of local states
5. An interaction potentially changes the topological organization of state

Thanks

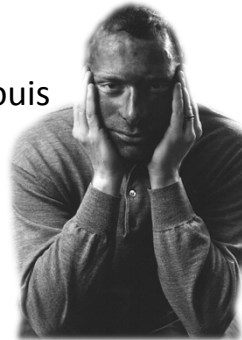
- Jean-Louis
- Antoine Spicher
- Olivier Michel

<http://mgs.spatial-computing.org>

- **PhD and other students**

Julien, Antoine, P. Barbier de Reuille,
T. Louail, E. Delsinne, V. Larue, F. Letierce,
B. Calvez, F. Thonerieux, D. Boussié,
iGem'07 Paris team, *and the others...*

Jean-Louis



Antoine



Olivier



- **Some past and present collaborations**

- A. Lesne (IHES, stochastic simulation)
- P. Prusinkiewicz (Calgary, declarative modeling)
- C. Godin (CIRAD, biological modeling)
- H. Berry (LRI, stochastic simulation)
- G. Malcolm (Liverpool, rewriting)
- J.-P. Banâtre (IRISA, programming)
- P. Fradet (InriaAlpes, programming)
- F. Delaplace (IBISC, synthetic biology)
- D. Pumain (Géographie-Cité, city growth)
- R. Doursat (ISC, morphogenetic engineering)
- F. Gruau (U. PXL, language and hardware)
- P. Liehnard (Poitiers, CAD, Gmap and quasi-manifold)

